

## 13.5 Turing Machines

### 13.5 pg. 897 # 1

Let  $T$  be the Turing machine defined by the five-tuples:  $(s_0, 0, s_1, 1, R)$ ,  $(s_0, 1, s_1, 0, R)$ ,  $(s_0, B, s_1, 0, R)$ ,  $(s_1, 0, s_2, 1, L)$ ,  $(s_1, 1, s_1, 0, R)$ , and  $(s_1, B, s_2, 0, L)$ . For each of these initial tapes, determine the final tape when  $T$  halts, assuming that  $T$  begins in initial position.

a )

	B	B	0	0	1	1	B	B	
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b )

	B	B	1	0	1	B	B	B	
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d )

	B	B	B	B	B	B	B	B	
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### 13.5 pg. 898 # 3

What does the Turing machine described by the five-tuples  $(s_0, 0, s_0, 0, R)$ ,  $(s_0, 1, s_1, 0, R)$ ,  $(s_0, B, s_2, B, R)$ ,  $(s_1, 0, s_1, 0, R)$ ,  $(s_1, 1, s_0, 1, R)$ , and  $(s_1, B, s_2, B, R)$  do when given

- 11 as input?
- an arbitrary bit string as input?

### 13.5 pg. 898 # 7

Construct a Turing machine with tape symbols 0, 1, and  $B$  that, when given a bit string as input, replaces the first 0 with a 1 and does not change any of the other symbols on the tape.

### 13.5 pg. 898 # 9

Construct a Turing machine with tape symbols 0, 1, and  $B$  that, when given a bit string as input, replaces all but the leftmost 1 on the tape with 0s and does not change any of the other symbols on the tape.

### 13.5 pg. 898 # 11

Construct a Turing machine that recognizes the set of all bit strings that end with a 0.

**13.5 pg. 898 # 13**

Construct a Turing machine that recognizes the set of all bit strings that contain an even number of 1s.

**13.5 pg. 898 # 19**

Construct a Turing machine that computes the function  $f(n) = n - 3$  if  $n \geq 3$  and  $f(n) = 0$  for  $n = 0, 1, 2$  for all nonnegative integers  $n$ .